

## Crystal Structures, Electronic Structures, and Physical Properties of $Tl_4MQ_4$ (M = Zr or Hf; Q = S or Se)

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The ternary thallium chalcogenides of the general formula  $Tl_4MQ_4$  (M = Zr or Hf; Q = S or Se) were obtained from high-temperature reactions without air. These sulfides and selenides are isostructural, crystallizing in the triclinic system with space group  $P\bar{1}$  and  $Z = 5$ , in contrast to  $Tl_4MTe_4$  compounds that adopt space group  $R\bar{3}$ . The unit cell parameters for  $Tl_4ZrS_4$  are as follows:  $a = 9.0370(5)$  Å,  $b = 9.0375(5)$  Å,  $c = 15.4946(9)$  Å,  $\alpha = 103.871(1)^\circ$ ,  $\beta = 105.028(1)^\circ$ ,  $\gamma = 90.138(1)^\circ$ , and  $V = 1183.7(1)$  Å<sup>3</sup>. In contrast to the corresponding tellurides, the sulfides and selenides exhibit edge-shared  $MQ_6$  octahedra, propagating along the  $c$  axis in a zigzag manner. All elements occur in the most common oxidation states, according to the formulation  $(Tl^+)_4(M^{4+})(Q^{2-})_4$ . Electronic structure calculations predict energy band gaps of 1.7 eV for  $Tl_4ZrS_4$  and 1.3 eV for  $Tl_4ZrSe_4$ , which are in accordance with the large resistivity values observed experimentally.

### Introduction

Heavy metal chalcogenides have attracted an increasing level of attention because of their promising thermoelectric properties.<sup>1–4</sup> Some of the well-known Tl-based thermoelectrics are  $Tl_9AgTe_5$  (figure of merit  $ZT = 1.2$  at 700 K),<sup>5</sup>  $Tl_9BiTe_6$  ( $ZT = 1.2$  at 500 K),<sup>6</sup>  $TlSbTe_2$  ( $ZT = 0.87$  at 715 K),<sup>7</sup>  $Tl_4SnTe_3$  ( $ZT = 0.74$  at 673 K),<sup>8</sup> and  $Tl_4PbTe_3$  ( $ZT = 0.71$  at 673 K).

Recently, we began to explore some thallium-rich chalcogenides that contain group 4 metal atoms such as Zr and Hf. Our first result was the discovery of two new thallium–group 4–telluride compounds,  $Tl_4MTe_4$  (M = Zr and Hf) that comprise triple units of face-condensed  $MTe_6$  distorted octahedra.<sup>9</sup> Several ternary thallium or alkali metal chalcogenides of such 4-1-4 formulas, with group 4 or group 14 elements,

have been identified.<sup>10–15</sup>  $Na_4SnS_4$  and  $Na_4SnSe_4$  are isostructural (space group  $P\bar{4}2_1c$ ), whereas  $K_4SnSe_4$  ( $Pnma$ ) is different<sup>11</sup> and in turn isostructural with  $Na_4SiSe_4$ .<sup>16</sup>  $Na_4TiSe_4$  adopts another different structure in space group  $I2/a$ .<sup>10</sup> All of these  $A_4M'Q_4$  compounds (A = Na or K; M' = Si, Ge, Sn, or Ti) are composed of isolated tetrahedral anionic  $[M'Q_4]^{4-}$  units. Some Tl-based chalcogenides of the series  $Tl_4M'Q_4$  (M' = Ti, Si, Ge, or Sn; Q = S or Se) are also known to exist.<sup>13–15</sup>  $Tl_4TiQ_4$  and  $Tl_4SnQ_4$  crystallize in the monoclinic crystal system with space group  $P2_1/c$ ;<sup>13</sup>  $Tl_4SiS_4$  and  $Tl_4GeS_4$  are reported to adopt space group  $Cc$ ,<sup>14,15</sup> and  $Tl_4SiSe_4$  is reported to adopt space group  $C2/c$ .<sup>14</sup> This  $Tl_4M'Q_4$  series also shares the  $[M'Q_4]^{4-}$  units mentioned above that are separated by Tl atoms. In all these cases, weakly bonding Tl–Tl contacts are between 3.4 and 4.0 Å in length. Some of these ternary thallium–group 4–chalcogenide compounds show interesting thermoelectric properties as well.<sup>9,17</sup>

There have been few reports about the structure and properties of the Zr or Hf counterparts of the chalcogenides mentioned above. Phase diagram studies of the  $Tl_2Q$ – $ZrQ_2$  (Q = S, Se, or Te) systems<sup>18</sup> pointed toward the existence of  $Tl_4ZrS_4$  and  $Tl_4ZrSe_4$ , but not  $Tl_4ZrTe_4$ , while no such studies

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Table 1. Crystallographic Data of Tl<sub>4</sub>MQ<sub>4</sub>

formula	Tl <sub>4</sub> ZrS <sub>4</sub>	Tl <sub>4</sub> HfS <sub>4</sub>	Tl <sub>4</sub> ZrSe <sub>4</sub>	Tl <sub>4</sub> HfSe <sub>4</sub>
formula weight (g/mol)	1036.94	1124.21	1224.54	1311.81
<i>T</i> of measurement (K)	296(2)	296(2)	296(2)	296(2)
wavelength (Å)	0.71073	0.71073	0.71073	0.71073
crystal system	triclinic	triclinic	triclinic	triclinic
space group	<i>P</i> $\bar{1}$	<i>P</i> $\bar{1}$	<i>P</i> $\bar{1}$	<i>P</i> $\bar{1}$
<i>a</i> (Å)	9.0370(5)	9.032(1)	9.274(2)	9.288(8)
<i>b</i> (Å)	9.0375(5)	9.035(1)	9.264(2)	9.271(8)
<i>c</i> (Å)	15.4946(9)	15.448(2)	16.007(3)	16.01(1)
$\alpha$ (deg)	103.871(1)	103.768(2)	104.146(3)	104.11(1)
$\beta$ (deg)	105.028(1)	104.759(2)	105.326(3)	105.05(1)
$\gamma$ (deg)	90.138(1)	90.125(2)	90.219(3)	90.09(1)
<i>V</i> (Å <sup>3</sup> )	1183.7(1)	1181.2(2)	1282.7(5)	1288(2)
<i>Z</i>	5	5	5	5
$\rho_{\text{calcd}}$ (g/cm <sup>3</sup> )	7.273	7.902	7.926	8.458
no. of collected, unique, observed reflections ( <i>R</i> <sub>int</sub> )	16813, 6867, 5377 (0.056)	9118, 6337, 4970 (0.033)	12888, 7296, 4460 (0.045)	9280, 6715, 3304 (0.074)
<i>R</i> <sub>1</sub> / <i>wR</i> <sub>2</sub> [ <i>I</i> > 2 $\sigma$ ( <i>I</i> )] <sup>a</sup>	0.042/0.089	0.065/0.139	0.068/0.111	0.108/0.236

$$^a R_1 = \sum ||F_o| - |F_c|| / \sum |F_o|; wR_2 = \{ \sum [w(F_o^2 - F_c^2)^2] / \sum [w(F_o^2)^2] \}^{1/2}.$$

on the Hf counterparts were performed to the best of our knowledge. With this contribution, we present the crystal structures, electronic structures, and electrical resistance of Tl<sub>4</sub>ZrS<sub>4</sub>, Tl<sub>4</sub>HfS<sub>4</sub>, Tl<sub>4</sub>ZrSe<sub>4</sub>, and Tl<sub>4</sub>HfSe<sub>4</sub>.

## Experimental Section

**Syntheses and Analyses.** The target compositions were synthesized from the constituent elements stored in an argon-filled glovebox [Tl granules, 99.9% (Alfa Aesar); Zr powder, 325 mesh, 98.5% (including 2% Hf) (Alfa Aesar); Hf powder, 100 mesh, 99.8% (including 1% Zr) (Alfa Aesar); and Te chunks, 99.9% (Aldrich)]. The elements were loaded in the required stoichiometry into glassy carbon crucibles, which were then introduced into silica ampules and sealed under vacuum. These ampules were heated slowly to 1073 K in a resistance furnace, allowed to remain at 1073 K for 100 h, and finally slowly cooled to room temperature. To analyze the phase purity, we measured the powder X-ray patterns of the samples using an Inel powder diffractometer with a position-sensitive detector and Cu K $\alpha_1$  radiation. In case of the sulfides, all reflections belonged to the title compounds, Tl<sub>4</sub>MS<sub>4</sub>, while minor unidentified reflections were present in the case of the selenides in addition to those of the target compounds. The samples exhibited no noticeable reaction under ambient conditions in air.

The glassy carbon crucibles are not required for the formation of Tl<sub>4</sub>MQ<sub>4</sub>, but their presence prevents tube attack; the first reactions without these crucibles yielded high but not 100% yields of all four Tl<sub>4</sub>MQ<sub>4</sub> chalcogenides, while the samples were sticking to the silica walls. This method led to the formation of Tl<sub>6</sub>Si<sub>2</sub>Te<sub>6</sub> as a very minor side product during attempts to prepare Tl<sub>4</sub>ZrTe<sub>4</sub>.

Energy dispersive X-ray analysis (EDAX) using the LEO 1530 electron microscope with an additional EDAX device, EDAX Pegasus 1200, revealed the presence of the three elements, Tl, M, and Q, approximately in the expected 4:1:4 ratio.

The thermal behavior of these materials was studied via differential scanning calorimetry using the Netzsch STA 409PC Luxx instrument in an argon atmosphere as described previously.<sup>19</sup> Both sulfides melt congruently around 1000 K (Tl<sub>4</sub>ZrS<sub>4</sub>) and 984 K (Tl<sub>4</sub>HfS<sub>4</sub>), whereas the selenides melt incongruently around 797 K (both Tl<sub>4</sub>ZrSe<sub>4</sub> and Tl<sub>4</sub>HfSe<sub>4</sub>). The latter explains the presence of minor side products as well as the poor crystal quality in the case of the selenides. These results are in qualitative agreement with the work on the Tl<sub>2</sub>Q–ZrQ<sub>2</sub> phase diagrams mentioned above,<sup>18</sup> wherein the respective melting and/or

decomposition points were determined to be 985 K for Tl<sub>4</sub>ZrS<sub>4</sub> and 805 K for Tl<sub>4</sub>ZrSe<sub>4</sub>.

**Single-Crystal Structure Determinations.** Suitable single crystals (rectangular blocks or plates) were picked from the respective bulk sample for the single-crystal X-ray diffraction analysis. The data were collected at room temperature using a Bruker Smart Apex CCD diffractometer that employs Mo K $\alpha$  radiation, by scans of 0.3° in  $\omega$  at three different  $\phi$  angles with exposure times of 30 s each for a total of 3 × 600 frames in each case. The data were treated for Lorentz and polarization corrections. The absorption corrections were based on fitting a function to the empirical transmission surface as sampled by multiple equivalent measurements. The APEX II package,<sup>20</sup> which includes SAINT<sup>21</sup> and SHELXTL,<sup>22</sup> was used for the data reduction and structure refinement.

The single-crystal X-ray diffraction analysis of the crystal picked from the Tl<sub>4</sub>ZrS<sub>4</sub> batch showed that the compound crystallizes in the triclinic system, with space group *P* $\bar{1}$ . After the successful structure solution and refinement, we tentatively refined the occupancies of the Tl atom sites, although the thermal expansion parameters were inconspicuous. The lowest Tl site occupancy [Tl3, 0.985(3)] was equal to full occupancy within 5 times its standard deviation. Next, we fixed all Tl occupancies at 1.0 and refined the Zr occupancies, resulting in values between 1.000(4) and 1.014(3). Hence, all occupancies were kept at 1.0 in the final refinement. Finally, ADDSYM was used to check for any missed symmetry, and the atomic positions were standardized with TIDY within the PLATON package.<sup>23</sup> The highest remaining peak of the electron density synthesis of 3.3 e/Å<sup>3</sup> was located only 0.8 Å from Tl7, and the deepest hole of –4.4 e/Å<sup>3</sup> was 0.8 Å from Tl4.

Single crystals of Tl<sub>4</sub>HfS<sub>4</sub>, Tl<sub>4</sub>ZrSe<sub>4</sub>, and Tl<sub>4</sub>HfSe<sub>4</sub> were also analyzed, and all of them (while of a poorer quality because of their incongruent melting and small crystal sizes) were found to be isostructural with Tl<sub>4</sub>ZrS<sub>4</sub>. The crystallographic data of all four compounds are listed in Table 1, and the atomic positions and equivalent displacement parameters of Tl<sub>4</sub>ZrS<sub>4</sub> are listed in Table 2.

**Electronic Structure Calculations and Electrical Resistivity Measurements.** The electronic structure calculations were performed using the self-consistent tight binding first-principles linear muffin-tin orbital (LMTO) method that uses the atomic

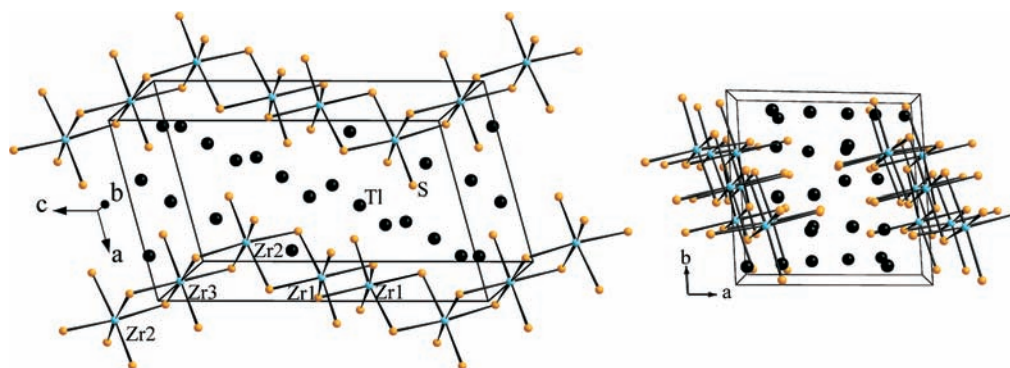
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**Figure 1.** Crystal structure of  $\text{Tl}_4\text{ZrS}_4$  viewed along the  $b$  (left) and  $c$  (right) axes. Tl–S bonds have been omitted for the sake of clarity.

**Table 2.** Atomic Positions and Equivalent Displacement Parameters<sup>a</sup> of  $\text{Tl}_4\text{ZrS}_4$

atom	site	$x$	$y$	$z$	$U_{\text{eq}}$ ( $\text{\AA}^2$ )
Tl1	2i	0.05058(5)	0.08212(5)	0.80084(3)	0.0230(1)
Tl2	2i	0.22063(5)	0.72301(5)	0.40061(3)	0.0230(1)
Tl3	2i	0.22368(5)	0.08791(5)	0.59828(3)	0.0240(1)
Tl4	2i	0.22668(5)	0.44869(5)	0.79582(3)	0.0222(1)
Tl5	2i	0.37987(5)	0.09446(5)	0.39232(3)	0.0247(1)
Tl6	2i	0.39207(5)	0.70404(5)	0.19360(3)	0.0243(1)
Tl7	2i	0.41442(5)	0.46169(5)	0.59957(3)	0.0238(1)
Tl8	2i	0.58003(5)	0.09753(5)	0.19975(3)	0.0237(1)
Tl9	2i	0.60692(5)	0.72061(5)	0.00129(3)	0.0231(1)
Tl10	2i	0.77123(5)	0.09999(5)	0.00683(3)	0.0233(1)
Zr1	2i	0.0175(1)	0.6827(1)	0.59971(6)	0.0114(2)
Zr2	2i	0.1745(1)	0.3075(1)	0.19931(6)	0.0116(2)
Zr3	1c	0	0.5	0	0.0122(3)
S1	2i	0.0600(3)	0.0497(3)	0.4033(2)	0.0164(5)
S2	2i	0.0679(3)	0.3937(3)	0.5789(2)	0.0133(5)
S3	2i	0.0704(3)	0.2308(3)	0.0201(2)	0.0124(5)
S4	2i	0.0889(3)	0.5818(3)	0.1792(2)	0.0134(5)
S5	2i	0.2386(3)	0.0352(3)	0.1955(2)	0.0162(5)
S6	2i	0.2525(3)	0.3861(3)	0.3783(2)	0.0140(5)
S7	2i	0.4431(3)	0.3784(3)	0.1962(2)	0.0166(5)
S8	2i	0.7098(3)	0.2484(3)	0.3958(2)	0.0158(5)
S9	2i	0.7257(3)	0.4292(3)	0.0025(2)	0.0168(5)
S10	2i	0.9022(3)	0.2635(3)	0.2223(2)	0.0131(5)

<sup>a</sup>  $U_{\text{eq}}$  is defined as one-third of the trace of the orthogonalized  $U_{ij}$  tensor.

spheres approximation (ASA).<sup>24,25</sup> In this method, the density functional theory (DFT) is employed, which utilizes the local density approximation (LDA) for the exchange and correlation energies. The following wave functions were used: 6s, 6p, 6d, and 5f for Tl (the latter two downfolded<sup>26</sup>); 5s, 5p, 4d, and 4f for Zr (4f downfolded); 3s, 3p, and 3d for S (3d downfolded); and 4s, 4p, and 4d for Se (4d downfolded). The eigenvalue problems were solved on the basis of 132  $k$  points selected with an improved tetrahedron method<sup>27</sup> within the irreducible wedge of the first Brillouin zone. The electrical resistivity measurements were performed using a standard four-probe method, employing a Keithley 2400 source/measure unit.

**Crystal Structure.** The title compounds are isostructural. Here we focus on  $\text{Tl}_4\text{ZrS}_4$  as their representative. Its structure contains three crystallographically distinct Zr atoms, which are octahedrally (distorted) coordinated by S atoms. These  $\text{ZrS}_6$  octahedra are edge-shared to form a zigzag chain running along the  $c$  axis (left part of Figure 1). Therein, the metal atom sequence is  $-\text{Zr2}-\text{Zr3}-\text{Zr2}-\text{Zr1}-\text{Zr1}-$ . The edge-shared octahedra form

**Table 3.** Selected Interatomic Interactions of  $\text{Tl}_4\text{ZrS}_4$

	CN	distance range ( $\text{\AA}$ )	PBO <sup>a</sup>	valence sum <sup>b</sup>
Tl1–S	5	2.837(3)–3.297(2)	0.58	0.47
Tl2–S	5	2.931(2)–3.289(3)	0.54	0.39
Tl3–S	4	2.838(3)–3.147(2)	0.59	0.51
Tl4–S	5	2.897(3)–3.325(3)	0.59	0.45
Tl5–S	4	2.901(3)–3.270(3)	0.59	0.49
Tl6–S	4	2.885(3)–3.299(3)	0.60	0.52
Tl7–S	5	2.846(3)–3.261(2)	0.55	0.42
Tl8–S	4	2.833(3)–3.170(3)	0.59	0.51
Tl9–S	4	2.849(3)–3.275(3)	0.59	0.51
Tl10–S	5	2.886(2)–3.300(3)	0.55	0.40
Zr1–S	6	2.520(3)–2.642(3)	4.32	2.17
Zr2–S	6	2.520(3)–2.664(3)	4.20	2.08
Zr3–S	6	2.571(3)–2.600(2)	4.16	2.01

<sup>a</sup> Cumulated Pauling bond order. <sup>b</sup> Total bond-valence sum.

triple units, in which the Zr atoms (Zr2–Zr3–Zr2) are arranged in a linear fashion (the angle being  $180^\circ$ ). Two such units are connected by a dimeric edge-shared unit of  $\text{Zr1S}_6$  octahedra, with a  $\text{Zr3}-\text{Zr2}-\text{Zr1}$  angle of  $122^\circ$ .

These chains are separated from each other by the Tl atoms along the  $a$  and  $b$  axes (right part of Figure 1). The Zr–S bond lengths vary from 2.52 to 2.66  $\text{\AA}$  (Table 3), which are within the normal range of Zr–S distances as in  $\text{ZrS}_2$  of 2.57  $\text{\AA}$ .<sup>28</sup> The corresponding Zr–Se bonds are significantly longer because of the larger atomic radius of Se, and the Hf–Q bonds are generally slightly shorter than the corresponding Zr–Q bonds because of the slightly smaller atomic radius of Hf, compared to that of Zr.

The Zr–Zr distances within the chains of  $\text{Tl}_4\text{ZrS}_4$  are 3.82  $\text{\AA}$  (Zr2–Zr3), 3.92  $\text{\AA}$  (Zr3–Zr1), and 3.89  $\text{\AA}$  (Zr1–Zr1) and thus too long for significant interactions. The same is true for the S–S distances, which are all greater than 3.4  $\text{\AA}$ . Therefore, standard formal charges according to  $(\text{Tl}^+)_4\text{Zr}^{4+}(\text{S}^{2-})_4$  can be assumed.

The Tl–S distances range from 2.83 to 3.30  $\text{\AA}$  in  $\text{Tl}_4\text{ZrS}_4$ , comparable with those in  $\text{Tl}_4\text{M}'\text{Q}_4$  ( $\text{M}' = \text{Ti}, \text{Si}, \text{or Sn}$ ) of 2.90–3.45  $\text{\AA}$ .<sup>13,14</sup> Of the 10 crystallographically independent Tl sites, five (Tl1, Tl2, Tl4, Tl7, and Tl10) are connected to five S atoms and the remaining five to four S atoms each. Moreover, numerous Tl–Tl contacts as short as 3.69  $\text{\AA}$  exist. The coordination spheres around all Tl atoms are severely distorted because of the lone pair effect (filled 6s orbital) of  $\text{Tl}^+$  (Figure 2).

To look for systematic differences between the 4- and 5-fold coordinated Tl atoms, we performed bond-valence sum calculations according to the work of Pauling<sup>29</sup> and Brese and

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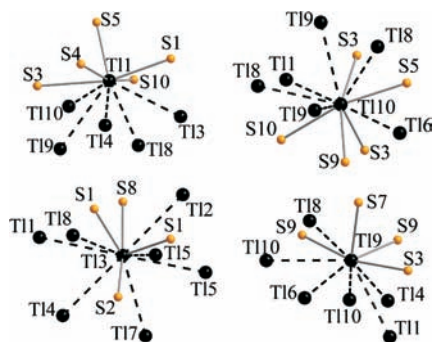


Figure 2. Selected Tl coordination spheres of  $\text{Tl}_4\text{ZrS}_4$ .



Figure 3. Tl atom network in the structure of  $\text{Tl}_4\text{ZrS}_4$ . Zr and S atoms have been omitted for the sake of clarity.

O'Keeffe.<sup>30</sup> The Pauling bond orders,  $\text{PBO}_{ij}$ , were calculated for each bond via the relationship  $\text{PBO}_{ij} = \exp[(R_{ij}^{\text{P}} - d_{ij})/0.6 \text{ \AA}]$  and the bond valences,  $v_{ij}$ , via the relationship  $v_{ij} = \exp[(R_{ij}^{\text{P}} - d_{ij})/0.37 \text{ \AA}]$ , where  $d_{ij}$  is the distance between the two selected atoms,  $R_{ij}^{\text{P}}$  is the sum of their single-bond Pauling radii, and  $R_{ij}$  is empirically derived from a comparison of known sulfides to be 2.63 Å for Tl–S bonds and 2.41 Å for Zr–S bonds.<sup>30</sup> When  $r_{\text{Tl}} = 1.44 \text{ \AA}$ ,  $r_{\text{Zr}} = 1.45 \text{ \AA}$ , and  $r_{\text{S}} = 1.04 \text{ \AA}$ , we obtain an  $R_{ij}^{\text{P}}$  values of 2.48 Å for Tl–S bonds and 2.49 Å for Zr–S bonds. Then, the  $\text{PBO}_{ij}$  and  $v_{ij}$  values were summed to obtain total bond orders and valence sums, respectively, as listed in Table 3 for  $\text{Tl}_4\text{ZrS}_4$ . In all cases, the cumulated Pauling bond orders were higher than the bond-valence sums, the latter being much smaller than expected, between 0.39 and 0.52 for the Tl atoms and between 2.01 and 2.17 for the Zr atoms. For the latter, the PBOs (4.16–4.32) are quite consistent and close to the expected value of 4. The PBOs of the Tl atoms are smaller than expected, and the 4-fold coordinated atoms appear to have slightly higher values (0.59–0.60) than the 5-fold ones (0.54–0.59). The same trend occurs in the valence sums (0.49–0.52 vs 0.39–0.47).

The Tl–Tl contacts with distances ranging from 3.69 to 3.99 Å may be considered to be weak interactions when compared to the strong Tl–Tl bonding in elemental Tl and weak interactions in Tl tellurides such as  $\text{Tl}_5\text{Te}_3$ ,<sup>31</sup>  $\text{Tl}_4\text{ZrTe}_4$ ,<sup>9</sup> and  $\text{Tl}_6\text{Si}_2\text{Te}_6$ .<sup>32</sup> The elemental (hexagonal) Tl has two different Tl–Tl distances of 3.41 and 3.46 Å, while these tellurides exhibit Tl–Tl interactions ranging from 3.49 to 4.03 Å in length. These weak Tl–Tl interactions of  $\text{Tl}_4\text{ZrS}_4$  result in chains of Tl atoms containing octahedra, cubes, and less regular rhomboids. These chains, running along the *b* axis, are interconnected via Tl7–Tl7 contacts of 3.99 Å to puckered slabs parallel to the *b*–*c* plane (Figure 3).

While  $\text{Tl}_4\text{ZrS}_4$  and  $\text{Tl}_4\text{ZrSe}_4$  are isostructural,  $\text{Tl}_4\text{ZrTe}_4$  adopts a unique structure type.<sup>9</sup> Therein,  $\text{ZrTe}_6$  octahedra are face-condensed unlike the edge-condensed  $\text{ZrQ}_6$  octahedra in  $\text{Tl}_4\text{ZrS}_4$  and  $\text{Tl}_4\text{ZrSe}_4$ , allowed by the larger size of the Te atoms

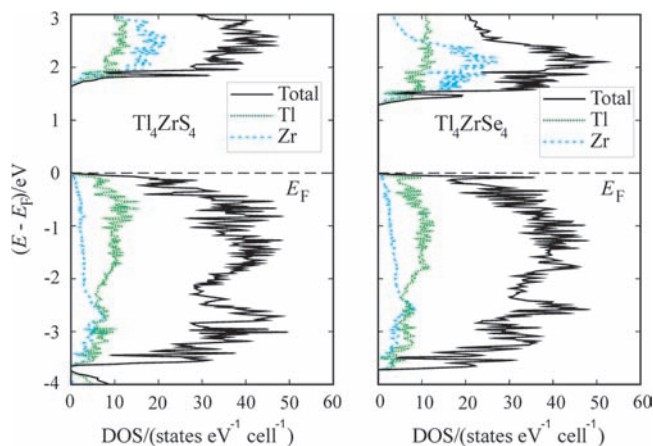


Figure 4. Densities of states for  $\text{Tl}_4\text{ZrS}_4$  (left) and  $\text{Tl}_4\text{ZrSe}_4$  (right).

compared to S and Se. A common feature of all these chalcogenides is the occurrence of a multitude of weak Tl–Tl contacts, resulting in a three-dimensional network of Tl atoms.

**Electronic Structure Calculations and Electrical Resistivity Measurements.** The densities of states (DOS) curves for  $\text{Tl}_4\text{ZrS}_4$  and  $\text{Tl}_4\text{ZrSe}_4$  are shown in Figure 4. Both materials appear to be semiconductors. The valence bands are extended over 3.5 eV and dominated by the S and Se p states, respectively. The Tl 6s states are located below these valence bands. The Tl and Zr contributions to the valence band are consequences of covalent mixing with the Q p states. The largest contributions to the conduction bands arise from the Zr 4d states.

The calculated band gap of  $\text{Tl}_4\text{ZrS}_4$  of 1.7 eV is in agreement with the high resistivity (on the order of  $10^7 \text{ \Omega cm}$  at room temperature) of the sample. The corresponding selenide has a smaller calculated band gap of 1.3 eV (room temperature resistivity of  $10^5 \text{ \Omega cm}$ ). The colors observed for both sulfides (dark red, corresponding to a gap of  $\sim 1.9 \text{ eV}$ ) and both selenides (black, corresponding to a gap of  $< 1.7 \text{ eV}$ ) also confirm the trend of the decreasing gap size from the sulfides to the selenides, noting that DFT calculations typically underestimate the gap size. Lastly, the stoichiometric tellurides,  $\text{Tl}_4\text{ZrTe}_4$  and  $\text{Tl}_4\text{HfTe}_4$ , were predicted to be narrow band gap semiconductors, with a band gap of approximately 0.3 eV, and determined to have room-temperature resistivity values of  $< 0.4 \text{ \Omega cm}$ .<sup>9</sup>

The integrated crystal orbital Hamilton populations, ICOHPs,<sup>33,34</sup> confirm that the Tl–Tl contacts are bonding as postulated before. For example, the ICOHP value of the Tl2–Tl5 bond with its 3.69 Å length is  $-0.11 \text{ eV}$ , and the longer Tl7–Tl7 bond of 3.99 Å also has a significant, albeit small, ICOHP of  $-0.04 \text{ eV}$ , indicative of a minor net bonding character. For comparison, the bonds in elemental Tl of 3.41 and 3.46 Å exhibit ICOHP values of  $-0.48$  and  $-0.42 \text{ eV}$ , respectively. Thus, the ICOHP value of the shortest Tl–Tl interaction in  $\text{Tl}_4\text{ZrS}_4$  amounts to 24% of the ICOHP average of the bonds of the element, confirming the weak but significant bonding character.

## Conclusions

Room-temperature single-crystal X-ray diffraction results revealed that the four chalcogenides of the formula  $\text{Tl}_4\text{MQ}_4$  ( $\text{M} = \text{Zr}$  or  $\text{Hf}$ ;  $\text{Q} = \text{S}$  or  $\text{Se}$ ) are isostructural, crystallizing in a new structure type. A zigzag chain of edge-sharing  $\text{MQ}_6$  octahedra and an infinite network of Tl atoms occur in these chalcogenides.

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With no Q–Q bonds present, all elements adopt their most common oxidation states, namely,  $Tl^+$ ,  $M^{4+}$ , and  $Q^{2-}$ . These materials are shown by calculation to be intrinsic semiconductors, supported by their dark red appearance in the case of the sulfides and the measured high room-temperature resistivity values in all cases. Thus, they cannot be used as thermoelectric materials. The corresponding tellurides exhibit an entirely different structure with face-sharing  $MTe_6$  octahedra and much smaller band gaps, resulting in promising thermoelectric properties as described previously.<sup>9</sup>

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**Supporting Information Available:** Four crystallographic information files (CIF). This material is available free of charge via the Internet at <http://pubs.acs.org>.